

ON TWO PROBLEMS FOR GAUSS COMPOUND MEAN

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Abstract. In this paper, we give answers to two open problems concerning Gauss Compound mean posed in the paper: [ZH. H. YANG, *A New Proof of Inequalities for Gauss Compound Mean*, Int. Journal of Math. Analysis, Vol. 4, (2010), no. 21, 1013–1018.] One of the problems is equivalent to the Vamanamurthy problem.

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