

INEQUALITIES VIA HARMONIC CONVEX FUNCTIONS: CONFORMABLE FRACTIONAL CALCULUS APPROACH

MUHAMMAD UZAIR AWAN, MUHAMMAD ASLAM NOOR,
MARCELA V. MIHAI AND KHALIDA INAYAT NOOR

Abstract. The main objective of this paper is to establish some conformable fractional estimates of Hermite-Hadamard type integral inequalities via harmonic convex functions.

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