

## REFINEMENTS AND GENERALIZATIONS OF MAJORIZATION, FAVARD AND BERWALD–TYPE INEQUALITIES VIA FINK IDENTITY

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*Abstract.* In this paper we present refinements of the majorization-type inequalities via an inequality obtained from a Fink's identity as well as the refinements of the Favard-Berwald type inequalities by using monotonic sequence and positive weights.

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