

SOME IMPROVED INEQUALITIES IN AN INNER PRODUCT SPACE

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Abstract. The aim of the paper is to present some improvements of an extended Cauchy-Schwarz inequality for four vectors in a real inner product space and derive certain consequences.

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