

## GENERALIZATION OF HEINZ OPERATOR INEQUALITIES VIA HYPERBOLIC FUNCTIONS

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*Abstract.* In this paper, we use the Taylor series of hyperbolic functions  $\cosh x$  and  $\sinh x$  to get some generalized inequalities for the Heinz operator means.

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