

## GEOMETRIC PROPERTIES OF MATHIEU–TYPE POWER SERIES INSIDE UNIT DISK

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*Abstract.* In the present investigation we study normalized Mathieu-type power series and find sufficient conditions, so that the normalized Mathieu-type power series have certain geometric properties like close-to-convexity and starlikeness inside the unit disc.

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