

OPTIMAL BOUNDS FOR THE TANGENT AND HYPERBOLIC SINE MEANS II

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Abstract. We provide the optimal bounds for the tangent and hyperbolic sine means in terms of various weighted means of the arithmetic and harmonic means.

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