

SOME INEQUALITIES INVOLVING OPERATOR MEANS AND MONOTONE CONVEX FUNCTIONS

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Abstract. Utilizing the Mond-Pečarić method and the properties of operator means, we present some Ando's type inequalities. Some inequalities in the existing literature are also generalized by our results.

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