

JENSEN–TYPE INEQUALITIES AND THEIR APPLICATIONS

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Abstract. In the present paper, we establish some entirely new Jensen-type discrete and integral inequalities. As applications of these results, we strengthen the well-known majorization theorem of Hardy, Littlewood and Pólya, and we also give a generalization of Andersson's inequality.

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