

ON UNICITY OF MEROMORPHIC FUNCTIONS CONCERNING THE SHIFTS AND DERIVATIVES

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Abstract. This paper is devoted to studying the sharing value problem for the derivative of a meromorphic function with its shift and q -difference. The results in the paper improve and generalize the recent result due to Qi, Li and Yang [28].

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