

MATRIX OSTROWSKI INEQUALITY VIA THE MATRIX GEOMETRIC MEAN

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Abstract. In this paper, we show a symmetric generalization of the Ostrowski inequality due to Fujii, Lin and Nakamoto. Moreover, we show its two variable extension. Inspired by this, we present matrix Ostrowski inequalities via the matrix geometric mean.

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