

A NEW PROOF OF PÓLYA–KNOPP'S INEQUALITY WITH AN EXTENSION

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Abstract. We show that a continuous version of Hölder's inequality can give a new and direct proof of the Pólya-Knopp type inequalities. We also have a single variable generalization of Pólya-Knopp's inequality.

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