

## ON THE PRODUCT OF CONTINUOUS PRIME NUMBERS

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**Abstract.** Basing on some deep conclusions of the prime number estimation, we give a fine from of the product of continuous prime numbers. These conclusions further improve the corresponding inequality of Panaitopol and more accurate conclusion is obtained.

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