

ON THE OPERATOR ACZÉL INEQUALITY AND ITS REVERSE

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Abstract. In this paper, we present some operator and eigenvalue inequalities involving operator monotone, doubly concave and doubly convex functions. These inequalities provide some variants of the operator Aczél inequality and its reverse via the generalized Kantorovich constant.

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