

THE APPLICATIONS OF SOME BASIC MATHEMATICAL INEQUALITIES ON THE CONVERGENCE OF THE PRIMITIVE EQUATIONS OF MOIST ATMOSPHERE

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Abstract. In this paper, we show the applications of some basic mathematical inequalities in partial differential equations. By using the differential inequality technique, the convergence of the primitive equations of moist atmosphere is obtained

Mathematics subject classification (2010): 35K05, 35K20, 35K55.

Keywords and phrases: Sobolev inequalities, convergence, primitive equations.

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