

SCHUR-CONVEXITY RELATED TO CO-ORDINATED CONVEX FUNCTIONS IN PLANE

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Abstract. In the paper, we investigate Schur-convexity of some functions which are obtained from the co-ordinated convex functions on a square in plane. A version of celebrated Leibniz's derivative formula for double integrals is also given.

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