

NON-CONFORMABLE INTEGRAL INEQUALITIES OF CHEBYSHEV-PÓLYA-SZEGÖ TYPE

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Abstract. Inequality studies involving new integrals and derivatives have been carried out recently. This article designed as follows, the results were obtained by using the non-conformable fractional integral operators to provide new inequalities of Polya-Szegö and Chebyshev type. Some special cases have been considered for our main findings.

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