

SOME INEQUALITIES ON THE INVERSE SUM INDEG COINDEX

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Abstract. Topological indices and coindices play an important role in mathematical chemistry. In this paper we establish some lower and upper bounds for the inverse sum indeg coindex in terms of different graph parameters associated with the structure of the graph. We also obtain relations between the inverse sum indeg coindex and some other indices and coindices.

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