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SINGULAR VALUES INEQUALITIES FOR MATRIX MEANS

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Abstract. In this article, we show multiple inequalities for the singular values of the difference of matrix means. The obtained results refine and complement some well established results in the literature. Although we target singular values inequalities, we will show several matrix means inequalities, as well.

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