

FURTHER NUMERICAL RADIUS INEQUALITIES

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Abstract. In this work, some numerical radius inequalities for Hilbert space operators are introduced. Namely, we applying the Hermite-Hadamard inequality and some other recent results by using the concept of operator convexity and superquadracity.

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