

## REVERSE FORM OF THE MINKOWSKI INEQUALITIES WITH APPLICATIONS

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*Abstract.* In this paper, we obtain the reverse of Minkowski inequality for matrices, and from this we give reverse forms of the Oppenheim inequality for  $n$ -simplices and the Neuberger-Pedoe inequality for triangles.

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