

## FRACTIONAL QUANTUM ANALOGUES OF TRAPEZOID LIKE INEQUALITIES

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*Abstract.* We derive two new fractional quantum integral identities. Using these identities we obtain several new fractional quantum estimates of trapezoid like inequalities essentially using the class of preinvex functions.

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