

## SHARPED JORDAN'S TYPE INEQUALITIES WITH EXPONENTIAL APPROXIMATIONS

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*Abstract.* In this paper, we establish two exponential double inequalities generalized Jordan's inequality.

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