# APPROXIMATION OF FUNCTIONS IN A WEIGHTED LEBESGUE SPACE BY MEANS OF THE PICARD SINGULAR INTEGRAL

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*Abstract.* The integral transforms, particularly singular integrals, play an important role in approximation theory. In this paper, we study the approximation properties of the Picard singular integral in a weighted Lebesgue space and weighted Hölder space. We also show that many of the theorems in the literature dealing with approximation of functions by the Picard singular integral are the special cases of our results.

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