

POLYNOMIAL DIFFERENTIATION COMPOSITION OPERATORS FROM H^p SPACES TO WEIGHTED-TYPE SPACES ON THE UNIT BALL

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Abstract. We characterize the boundedness, compactness, and estimate essential norm of a polynomial differentiation composition operator from the Hardy space H^p to the weighted-type spaces of holomorphic functions on the unit ball.

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