

## COMPLETE CONVERGENCE AND COMPLETE MOMENT CONVERGENCE FOR WEIGHTED SUMS OF $m$ -EXTENDED NEGATIVELY DEPENDENT RANDOM VARIABLES

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*Abstract.* The authors study the complete convergence and complete moment convergence for weighted sums of  $m$ -extended negatively dependent ( $m$ -END) random variables. The results obtained in this paper extend and improve the corresponding results of Wu, Zhai and Peng [Y. F. Wu, M. Q. Zhai and J. Y. Peng, On the complete convergence for weighted sums of extended negatively dependent random variables, *Journal of Mathematical Inequalities*, 13 (1) (2019), 251–260] and Zarei and Jabbari [H. Zarei and H. Jabbari, Complete convergence of weighted sums under negative dependence, *Statistical Papers*, 52 (2011), 413–418].

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