

## SINGULAR VALUE INEQUALITIES OF MATRICES WITH CONCAVE FUNCTIONS

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*Abstract.* In this note, we present some singular value inequalities of products and direct sums of matrices involving concave functions, which can be regarded as complements of some recent results in [Ann. Funct. Anal, 14 (2023) doi:10.1007/s43034-022-00233-1].

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