

FRAME INEQUALITIES IN HILBERT SPACES: TWO-SIDED INEQUALITIES WITH NEW STRUCTURES

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Abstract. This paper is devoted to establishing frame inequalities in Hilbert spaces. By using operator theory methods, several two-sided inequalities for frames are presented, which, comparing to previous inequalities on frames and generalized frames, admit new structures.

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