

STEVIĆ–SHARMA TYPE OPERATORS FROM H^∞ INTO THE BLOCH SPACE

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Abstract. In this paper, we give some characterizations for the boundedness and compactness of some Stević-Sharma type operators called the polynomial differentiation composition operators from H^∞ into the Bloch space on the unit disk.

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