

## LOWER BOUNDS FOR THE SMALLEST SINGULAR VALUE VIA PERMUTATION MATRICES

CHAOQIAN LI, XUELIN ZHOU AND HEHUI WANG\*

*Abstract.* We in this paper improve the well-known C. R. Johnson's lower bound for the smallest singular value via permutation matrices. A direct algorithm is also given to compute the new lower bound.

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