

ON THE GENERAL CASE OF BRANNAN CONJECTURE

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Abstract. We will prove the Brannan conjecture provided that the parameters α and β verify the conditions $\frac{3}{4} \leq \alpha \leq \beta \leq 1$. The basic tool of the study is a new integral representation deduced in this paper.

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