

LAI LAW FOR LINEAR PROCESSES WITH LONG MEMORY

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Abstract. The Lai law, characterizing the convergence rate of the single laws of logarithm for the sequence of independent and identically distributed random variables, has been extended to the linear processes with long memory.

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