

GENERAL NUMERICAL RADIUS INEQUALITIES FOR MATRICES OF HILBERT SPACE OPERATORS

MOHAMMED AL-DOLAT* AND KHALDOUN AL-ZOUBI

Abstract. We obtain new bounds for the numerical radius of certain $n \times n$ and general 2×2 operator matrices. We show that our bounds refines the bounds that are given in [1] and [3].

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