

EXTENSION OF (m, C) -ISOMETRIC COMMUTING MULTI-OPERATORS

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Abstract. This article examines the structural characteristics of a new class of so-called (n_1, \dots, n_d) -quasi- (m, C) -isometric commuting multioperators related to a given conjugation operator C on a Hilbert space \mathcal{H} .

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