

STRICT SINGULARITY OF VOLTERRA INTEGRAL OPERATOR ON BERGMAN–MORREY TYPE SPACES

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Abstract. In this paper, we study the strict singularity of the Volterra integral operator T_g (with symbol g) on Bergman–Morrey type spaces $A^{p,K}$. We show that compactness and strict singularity of T_g are equivalent on $A^{p,K}$.

Mathematics subject classification (2020): 30H99, 47B38.

Keywords and phrases: Volterra integral operator, strict singularity, Bergman–Morrey type space.

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