

STRONG DOUBLING CONDITIONS

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Abstract. We show that the class of strong doubling measures depends essentially on the parameter τ , and that the measure of the boundary layer of a QHBC domain decays geometrically, if the measure is suitably strong doubling.

Mathematics subject classification (1991): 28A75, 42B25.

Key words and phrases: Doubling condition, QHBC domain, maximal functions, covering lemmas.

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