

SOME EXPONENTIAL OPERATOR INEQUALITIES

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Abstract. We will simply show Ando's exponential inequality by making use of an approximation method and Furuta inequality, and then we will give some results about exponential inequalities.

Mathematics subject classification (1991): 47A63.

Key words and phrases: order of selfadjoint operators, Furuta inequality, norm derivative.

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