

A NOTE ON TWO THEOREMS OF LEINDLER

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Abstract. The theorem proved here is the generalization of two theorems of Leindler regarding embedding relations among classes of Fourier coefficients. The generalization is based on replacing the power functions by more general ones introduced by Mateljevič and Pavlovič.

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