

LOWER AND UPPER BOUNDS FOR THE PROBABILITY THAT AT LEAST r AND EXACTLY r OUT OF n EVENTS OCCUR

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Abstract. Lower and upper bounds are presented for the probability that at least r or exactly r out of n events occur, in terms of sums of joint probabilities of at most m events, where $m < n$.

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