

## A NOTE ON THE LEINDLER'S CLASS $S_\alpha$ , $\alpha > 0$

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*Abstract.* In this paper we generalize two inequalities of Telyakovskii type (see [2], [5], [6], [7]), by considering the class  $S_\alpha$ ,  $\alpha > 0$  (see [2]) and positive derivate of order  $\alpha$  for cosine and sine series. Also, an equivalent form of the Leinder's class  $S_\alpha$ ,  $\alpha > 0$  is given.

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