

## NEW ADVANCES ON THE GROTHENDIECK'S INEQUALITY PROBLEM FOR BILINEAR FORMS ON $JB^*$ -TRIPLES

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*Abstract.* We give a positive answer to the Barton-Friedman's conjecture on "Grothendieck's inequalities" for Cartan factors and  $JBW^*$ -triples.

*Mathematics subject classification (2000):* 17C65, 46K70, 46L05, 46L70.

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