

SOME INTERPOLATIONS AND REFINEMENTS OF HADAMARD'S INEQUALITY FOR r -CONVEX FUNCTIONS IN CARNOT GROUPS

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Abstract. Some nontrivial increasing functions will be interpolated in the Hadamard's inequality for r -convex function in Carnot groups. The methods are more natural and allow us to extend the condition $I^2(G) \cap C_{H,r}^w(G)$ to the condition $C(G) \cap C_{H,r}^w(G)$.

Mathematics subject classification (2000): 26D15, 49L25.

Key words and phrases: r -convex function, extended means; Carnot group, Hadamard's inequality, inequality.

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