

CERTAIN PROPERTIES ARISING FROM SOME INEQUALITIES CONCERNING SUBCLASSES OF MULTIVALENTLY ANALYTIC FUNCTIONS

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Abstract. In this investigation we prove several theorems involving a general class of multivalently analytic functions in the open unit disk. The applications of the main results are also considered for multivalently starlike functions and multivalently convex functions.

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