

A REMARK ON BETTER λ -INEQUALITY

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Abstract. We generalize the inequality of R. J. Bagby and D. S. Kurtz [1] to a wider class of potentials defined in terms of Young's functions. We make use of a certain submultiplicativity condition. We show that this condition cannot be omitted.

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