

NEW INEQUALITIES FOR MEANS IN TWO VARIABLES

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Abstract. In this paper, some bounds for $I(x, y)$ in terms of $A(x, y)$ and $L(x, y)$, and $L(x, y)$ in terms of $G(x, y)$ and $I(x, y)$ are established.

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