

## AN APPROACH TO KY FAN TYPE INEQUALITIES FROM BINOMIAL EXPANSIONS

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*Abstract.* In this article, using binomial expansions, we get some interesting recursive identities concerning arithmetic, geometric and harmonic means of positive numbers, from which, the most important Ky Fan type inequalities are handled by induction at once.

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