

## A NEW REFINED JORDAN'S INEQUALITY AND ITS APPLICATION

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*Abstract.* New refined lower and upper bound forms of Jordan's inequality are proved. As an application, the lower bound form is shown to improve L. Yang's inequality that plays a pivotal role in the theory of distribution of values of functions. Some numerical results are included.

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