

INTEGRAL REPRESENTATIONS OF GENERALIZED WHITELEY MEANS AND RELATED INEQUALITIES

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Abstract. The main purpose of this paper is to give two integral representations of generalized Whiteley means which are natural generalization of complete symmetric means. Various applications are given, mainly towards obtaining inequalities characteristic for complete symmetric means such as Schur's inequality. The Schur convexity of this means and related complete symmetric functions is also discussed.

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