

INEQUALITIES FOR THE C^* -VALUED NORM ON A HILBERT C^* -MODULE

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Abstract. The C^* -valued norm is defined on a Hilbert C^* -module by its standard inner product. In this paper we give generalizations of a number of classical inequalities known for either complex numbers or Hilbert space operators. In particular, we study Bohr's inequality for the C^* -valued norm on a Hilbert C^* -module.

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