

## INEQUALITIES ON REAL ROOTS OF POLYNOMIALS

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*Abstract.* We survey the most used bounds for positive roots of polynomials and discuss their efficiency. We obtain new inequalities on roots of polynomials. Then we give new inequalities on roots of orthogonal polynomials, obtained from the differential equations satisfied by these polynomials.

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